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Fermi surface reconstruction and electron dynamics at the charge-density-wave transition in TiSe_2

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The evolution of the charge carrier concentrations and mobilities are examined across the charge-density-wave (CDW) transition in TiSe_2 . Combined quantum oscillation and magnetotransport measurements show that a small electron pocket dominates the electronic properties at low temperatures while an electron and hole pocket contribute at room temperature. At the CDW transition, an abrupt Fermi surface reconstruction and a minimum in the electron and hole mobilities are extracted from two-band and Kohler analysis of magnetotransport measurements. The minimum in the mobilities is associated with the overseen role of scattering from the softening CDW mode. With the carrier concentrations and dynamics dominated by the CDW and the associated bosonic mode, our results highlight TiSe_2 as a prototypical system to study the Fermi surface reconstruction at a density-wave transition.

The electronic properties of transition metal dichalcogenides (TMDs) are of fundamental and practical interest. Many TMDs can be tuned between semimetallic, semiconducting, and insulating behaviour and thus allow to access a plethora of different electronic characteristics. In addition, ordered states, e.g. due to charge-density-wave (CDW) formation [1, 2] or superconductivity [3, 4] are present in many members of the family with open questions on the underlying mechanism. Many of these TMDs can be exfoliated to atomic monolayers providing new tuning parameters and novel physics through the reduced dimensionality [5–7].

TiSe_2 is a prototypical material for strong electronic interactions driving the CDW formation via a condensation of excitons, i.e. pairs of electrons and holes [8, 9]. Experimental and theoretical work have confirmed the relevance of the excitonic mechanism [10–12] which is widely accepted to work in cooperation with strong electron-phonon coupling [13–15].

Above the CDW transition temperature $T_{\text{CDW}} = 202\text{ K}$, TiSe_2 is characterised by small carrier concentrations stemming from up to three selenium-derived hole-like bands with cylindrical topology at the Γ point and a titanium-derived electron band with distorted and tilted ellipsoid topology present with 3-fold multiplicity at the L point [16–19] [20]. Whether these bands overlap in energy or have a band gap remains uncertain. Either way, the overlap or gap is small or comparable to thermal energies down to 50 K.

Below the CDW transition temperature, the electronic structure of TiSe_2 is dominated by a small electron pocket as shown by ARPES measurements [18]. Knowledge of how the electronic structure and electron dynamics evolve upon thermally melting the CDW in equilibrium, however, are outstanding. Several studies suggested that the Fermi surface reconstruction from the

CDW order and scattering associated with the CDW mode has a negligible effect on the electronic structure and dynamics [8, 19, 21, 22]. Rather a dominance of thermal occupation effects was suggested. In the past, studies of the charge carrier concentration were based on a single-band analysis of Hall effect and optical reflectivity measurements despite the evidence for two bands being present while no measurements distinguishing the electron and hole dynamics across T_{CDW} have been reported [23, 24]. Here, we use high-resolution magnetotransport and quantum oscillation (QO) measurements to extract the temperature dependence of the charge carrier concentration and mobility of the electron and hole band. We directly observe one quasi-ellipsoid Fermi surface at low temperatures which is identified as an electron pocket. This electron pocket and a hole pocket grow rapidly above 150 K showing evidence of an abrupt Fermi surface reconstruction and gapping of 75 % of the charge carrier concentration in the CDW state. At the same time, we observe a minimum in the mobility on both the electron and hole pocket at T_{CDW} highlighting the importance of scattering from the CDW forming phononic and/or electronic modes.

Single crystals of TiSe_2 were grown by chemical vapour transport at 580 °C as detailed in sec. SI of the Supplemental Material, and show a CDW transition at $T_{\text{CDW}} = 202\text{ K}$ consistent with other studies of high-quality samples [8, 25–28].

The low-temperature electronic structure of our TiSe_2 samples is dominated by an electron pocket as evident from the combination of quantum oscillation measurements and magnetotransport. The QO data shown in Fig. 1 reveal a single frequency $F = 0.26\text{ kT}$ for magnetic fields parallel to the crystallographic c direction, i.e. an orbit parallel to the basal plane. The increase of this frequency for orbits out of plane is well fitted by an ellip-

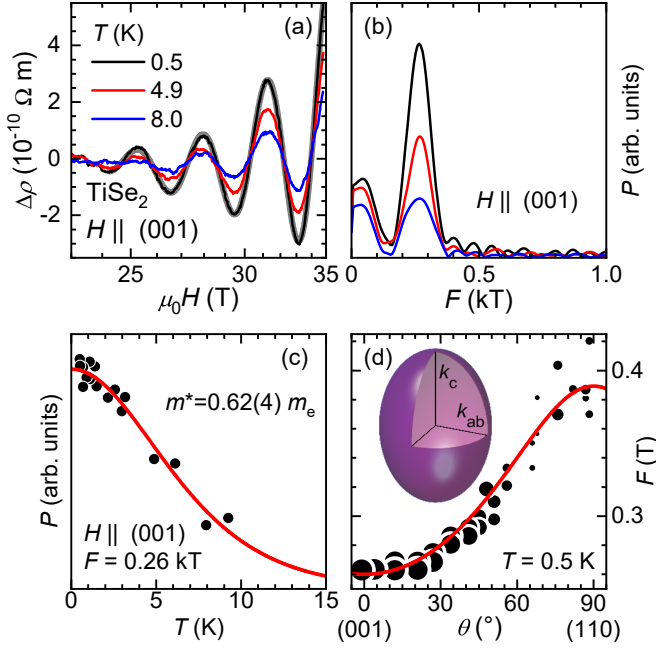


Figure 1. Quantum oscillations in TiSe_2 . (a) The oscillatory component of the resistivity $\Delta\rho$ obtained after subtraction of a linear background. The thick grey line is a fit of a single frequency with Dingle damping factor and quadratic background correction to the data at 0.5 K. (b) Fourier transform spectrum. (c) Temperature dependence of the amplitude. The red solid line is a Lifshitz-Kosevich fit to the data with an effective mass of $m_e^* = 0.62(4) m_e$, where m_e denotes the bare electron mass. (d) Dependence of the oscillation frequency on zenith angle θ for fixed azimuthal angle $\phi = 30^\circ$. Crystallographic directions are indicated on abscissa. Symbol size indicates oscillation amplitude. Solid red line represents a fit using an ellipsoid Fermi surface model as depicted in inset and described in section S III of the Supplemental Material.

oid shape (see Fig. 1(d) and S III of the Supplemental Material). This pocket is naturally associated with the L point electron pocket observed by ARPES studies [18].

Magnetotransport measurements confirm the electron-dominated character of our samples at low temperature as can be seen from the negative Hall resistivity ρ_{xy} in Fig. 2(a). Consistent with earlier reports [8, 29], ρ_{xy} changes sign smoothly around 190 K (cf. Fig. S2 of the Supplemental Material). The magnetoresistivity $\rho_{xx}(B)$ shown in Fig. 2(b-e) is small and positive. We use a two-band model with one electron and one hole band to simultaneously fit $\rho_{xx}(\mu_0 H)$ and $\rho_{xy}(\mu_0 H)$ [30]. The two-band fits shown as solid lines in Fig. 2 describe the data very well over the full temperature range.

The charge carrier concentrations n_e , n_h and mobilities μ_e , μ_h for the electron and hole band respectively are shown in Fig. 2 (f) and (g). The low-temperature value of n_e is in good agreement with our QO data and previous ARPES as well as heat capacity studies as summarised in Tab. S1 [30]. Thus the association of the observed QO

frequency with the electron pocket is confirmed. The electron pocket observed in our QO measurements accounts for virtually the full low-temperature electronic heat capacity (cf. Tab. S1) highlighting the dominance of the electron pocket at low T . The hole concentration extracted within the two-band model is very small at lowest temperatures and is likely to correspond to impurity states as indicated by the low hole mobility. We note that a free-electron single-band model cannot describe the low-temperature magnetotransport. Most notably, the Hall coefficient $R_H = -3.1 \times 10^{-7} \text{ m}^3 \text{ C}^{-1}$ measured at lowest temperatures does not match with a free electron estimate for the electron pocket based on the QO results of $R_H^{\text{QO}} = -1.75 \times 10^{-7} \text{ m}^3 \text{ C}^{-1}$.

At room temperature the electron and hole concentrations n_e and n_h are comparable in magnitude (cf. Fig. 2(f)). Above T_{CDW} , n_e and n_h are associated with the 3D-like electron pocket at the L point and the 2D-like hole pocket at the Γ point as seen by ARPES studies [17, 18]. The small linear temperature dependence of $n_e(T)$ and $n_h(T)$ above 210 K (dotted lines in Fig. 2(f)) is attributed to the varying thermal occupation of the two bands similar to the model of Watson et al. [21]. The slope of $n_e(T)$ and $n_h(T)$ at $T \geq T_{\text{CDW}}$ suggests a mass comparable to the free-electron mass for the electron band. The linear behaviour at high temperatures extrapolates to finite intercepts for both bands - these finite intercepts suggest a band overlap, i.e. not a gap, in the high-temperature phase above T_{CDW} .

The charge carrier concentrations show a sharp drop below T_{CDW} and saturate below 150 K. The drop is associated with condensation of electrons and holes into the CDW pair state and consequently with a Fermi surface reconstruction. The difference $\Delta n_{e,h} = n_{e,h}(T_{\text{CDW}}) - n_{e,h}(T = 0) = 4.2(2) \times 10^{25} \text{ m}^{-3}$ marks the loss of charge carriers and thus the density of electron-hole pairs. For $T < T_{\text{CDW}}$, $n_e(T)$ and $n_h(T)$ can be described by activated behaviour as shown by dashed lines in Fig. 2(f). Fits of exponential form yield a gap $\Delta_{\text{CDW}} = 75(1) \text{ meV}$, an energy scale consistent with $T_{\text{CDW}} = 202 \text{ K}$. The fact, that the exponential form fits the data even close to T_{CDW} suggests a finite gap up to T_{CDW} . A finite gap at T_{CDW} has indeed been seen in ARPES studies [32–34] where the total gap $\Delta = \Delta_{\text{CDW}} + \Delta_{\text{off}}$ is a sum of a BCS-like temperature dependent gap Δ_{CDW} with an onset at T_{CDW} on top of a weakly temperature dependent offset $\Delta_{\text{off}} \approx 70 \text{ meV}$. Our exponential fits are dominated by the temperature dependence of $n(T)$ just below T_{CDW} where $\Delta \approx \Delta_{\text{off}}$. The exponential form of $n_e(T)$ and $n_h(T)$ up to T_{CDW} and the good agreement of the gap value with Δ_{off} suggests a finite gap present above T_{CDW} potentially due to fluctuating electron-hole pairs that condense at T_{CDW} consistent with ARPES studies finding small intensity from backfolded bands above T_{CDW} [11].

The Fermi-surface reconstruction is further supported

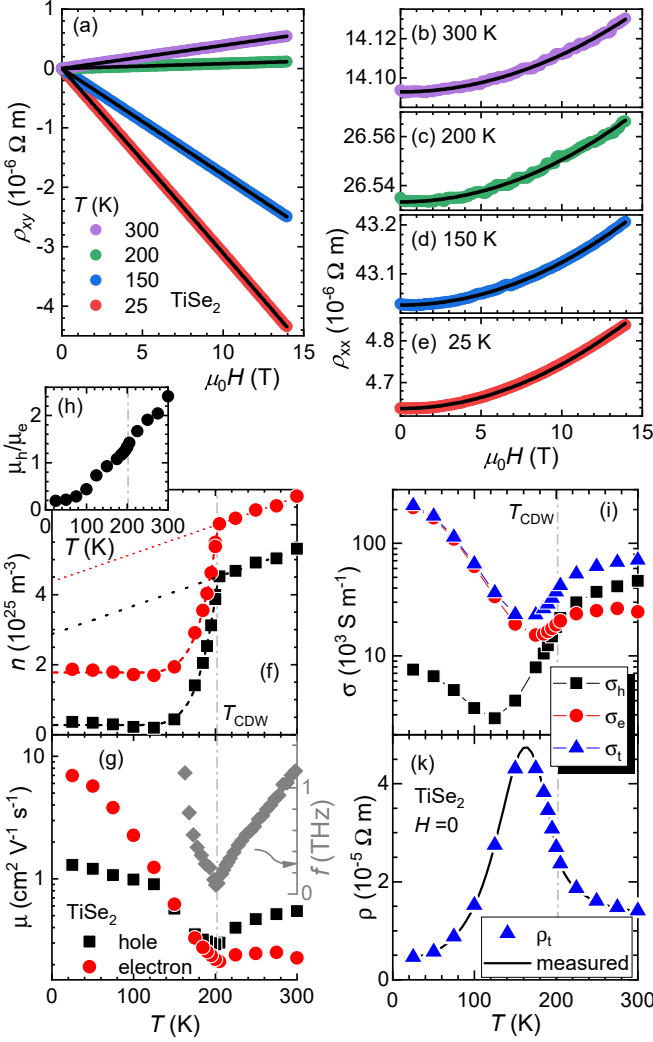


Figure 2. Two-band analysis of magnetotransport in TiSe_2 . Transversal (a) and longitudinal (b)-(e) resistivities of TiSe_2 at selected temperatures. Solid lines correspond to simultaneous two-band fits of both resistivities as described in S II of the Supplemental Material giving charge carrier concentrations (f) and mobilities (g) of the hole and electron band. (g) includes frequency of L -mode phonon from Ref [31] (adjusted for the reduced T_{CDW} of [31]). Dotted lines in (f) represent linear fits to $n_e(T)$ and $n_h(T)$ for $T \geq T_{\text{CDW}}$. Dashed lines represent fits of the form $n_{e,h}(T) = n_{(e,h)}(T=0) + A \exp(-2\Delta/k_B T)$. (h) Ratio of hole and electron mobility. Vertical dash-dotted line indicates T_{CDW} . Standard errors as obtained from the non-linear least-squares fits are smaller than symbol size. (i) Separate zero-field electron σ_e and hole band conductivity σ_h have been calculated from the mobilities and charge carrier concentrations shown in (f) and (g). Total conductivity is calculated as $\sigma_t = \sigma_e + \sigma_h$. Note the logarithmic scale. (k) Measured zero-field resistivity (solid line) compared to the calculated total resistivity $\rho_t = 1/\sigma_t$ (triangles). Solid line the represents measured resistivity.

by the Kohler analysis [35] presented in Fig. 3. The magnetoresistance follows a quadratic field dependence

at $T \geq 50$ K. However, the quadratic coefficient (Kohler slope) K shows a pronounced temperature dependence (cf. Fig. 3(b)). Above T_{CDW} , K is virtually constant and accordingly curves of MR vs $(\mu_0 H/\rho_0)^2$ collapse in Fig. 3(a). Below T_{CDW} , however, K rises very abruptly by more than an order of magnitude, passes a maximum at 150 K and saturates at a low-temperature value about double the room temperature value.

Kohler scaling and violations thereof have been observed in other CDW systems: In VSe_2 and NbSe_2 , separate Kohler scaling is present below and above T_{CDW} with a small difference in slope at T_{CDW} [36, 37]. In Ta_2NiSe_7 and NbSe_3 , Kohler scaling is only obeyed above T_{CDW} . In underdoped cuprate superconductors, Kohler scaling is observed at low temperature throughout T_{CDW} [38]. Our results on TiSe_2 show a larger change in K compared to other compounds because a larger fraction of the Fermi surface is affected by the CDW.

Our data suggest the Fermi surface reconstruction is the main reason for the violation of Kohler scaling in TiSe_2 . The sharp rise and strong temperature dependence of K below T_{CDW} can be due to (i) a reconstruction of the Fermi surface, (ii) an abrupt change in the anisotropy of the scattering time on the individual bands, or (iii) an abrupt change in the ratio of the scattering times of the electron and hole band, or a combination of the three. (iii) can be ruled out as this would manifest as an abrupt change of μ_h/μ_e which is not observed (Fig. 2(h)). (ii) may contribute to the change of K but it is unlikely to be the primary cause. For the violation of Kohler's law to be dominated by changes to scattering time anisotropy, a drastic and abrupt change to the phonon spectrum would be required. This is unlikely to occur independent of the Fermi surface reconstruction. A moderate change of the phonon spectrum may occur as a consequence of the Fermi surface reconstruction through the electron-phonon coupling. Thus, the sudden change of K at T_{CDW} is dominated by (i) a sudden reconstruction of the Fermi surface. This is in agreement with the sudden drop of the charge carrier concentrations (Fig. 2(f)).

The mobilities of the individual bands show very strong and non-trivial temperature dependencies Fig. 2(g). At room temperature, the hole mobility is larger than the electron mobility whilst this is reversed at lowest temperatures. Both mobilities have a minimum at T_{CDW} naturally associated with strong scattering from the softening mode associated with the CDW formation. Indeed, the temperature dependence of the mobilities show a dip similar in shape to the energy dependence of the L point phonon mode [31] (reproduced in Fig. 2(g)).

As noticed by Velebit et al. [23], the mobilities of the two bands are roughly equal at T_{CDW} as shown in Fig. 2(h). This equality highlights that scattering from the L point mode is the dominant process as the phase space for scattering from the electron to the hole band

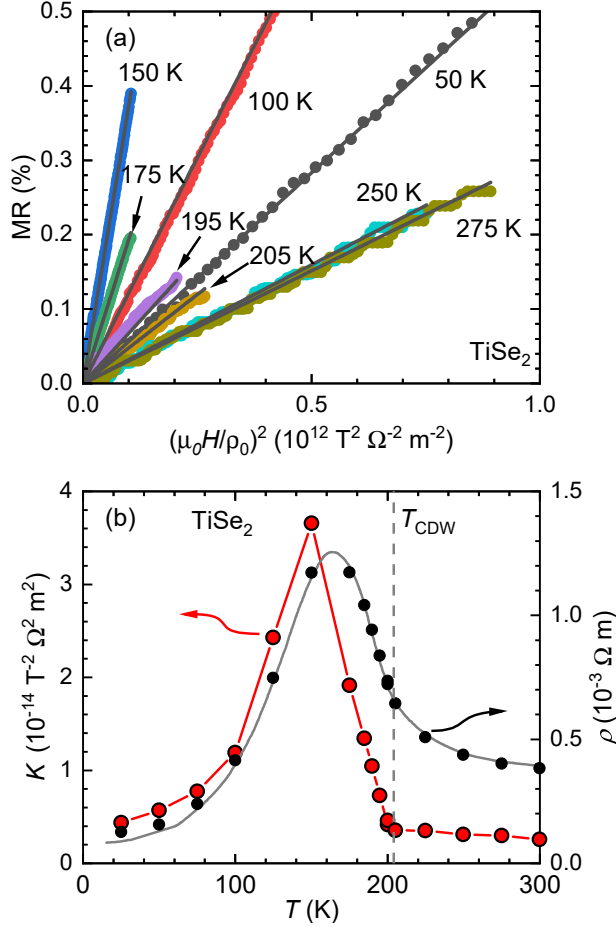


Figure 3. Kohler analysis of the magnetoresistance in TiSe_2 . (a) Magnetoresistance $\text{MR} = (\rho - \rho_0)/\rho_0$ plotted against $(\mu_0 H / \rho_0)^2$ where $\rho_0 = \rho(T, H = 0)$. Solid lines are linear fits of $\text{MR} = K (\mu_0 H)^2$. (b) The Kohler slope $K(T)$ (left axis) is shown with the solid red line as a guide to the eye. The zero-field resistivity $\rho_0(T)$ (black circles, right axis) is shown together with $\rho(T)$ from Ref. [8] (solid line) where the latter has been scaled to our data.

involves the density of states in both bands and the electron-phonon coupling.

The temperature dependence of the separated electron (σ_e) and hole (σ_h) conductivity are presented in Fig. 2(i). They show a minimum around $\approx 170 \text{ K}$ and $\approx 120 \text{ K}$, respectively. The total conductivity $\sigma_t = \sigma_e + \sigma_h$ and the total resistivity $\rho_t = 1/\sigma_t$ are dominated by σ_e and σ_h in different temperature regimes. The comparison of the thus calculated ρ_t and the measured $\rho_{xx}(H = 0)$ in Fig. 2(i) highlights the accuracy of the parameters extracted from the two-band fits.

From the temperature dependencies of the individual and total conductivities we identify that (i) at high temperature holes dominate the total conductivity and (ii) the negative $d\rho/dT$ above T_{CDW} is a consequence of the hole mobility increasing with temperature above T_{CDW} . (iii) The peak in $\rho(T)$ is dominated by the loss of a large

portion of charge carrier concentration of both holes and electrons due to the CDW with (iv) the positive $d\rho/dT$ at low temperatures arising due to the large increase in electron mobility towards lowest temperatures. (v) At low temperatures electrons dominate the conductivity. In summary, we conclude that the magnetotransport is dominated by the opening of the CDW gap and the scattering from the underlying bosonic mode.

Despite the smooth evolution of the resistivity, the magnetotransport behaviour provides direct evidence for an underlying abrupt Fermi surface reconstruction both as a large drop of the charge carrier concentrations and a sudden violation of Kohler's law below T_{CDW} . The analysis shows the loss of both electrons and holes below T_{CDW} highlighting the strong coupling between them. The fact that a large fraction of the charge carrier concentration is involved in the formation of the CDW enables a clear view at the electronic scattering associated with the L point CDW mode. The minimum in the mobility at T_{CDW} is a direct match to the softening of the L point mode and thus confirms that the dynamics of the charge carriers are directly linked to the dynamics of the CDW mode. Importantly, our measurements show that the strong scattering of the CDW mode causes the intriguing negative $d\rho/dT$ at room temperature. This makes TiSe_2 uniquely suitable to observe the strong coupling of the CDW mode to the electronic states. The scattering of electrons from the softening CDW mode is obscured in other prototypical CDW systems like NbSe_2 or VSe_2 where only small portions of the Fermi surface are matched by the ordering wave vector and only these "hot" parts experience strong scattering [39, 40]. Thus, TiSe_2 is a prototypical system to study the effects of a Fermi surface reconstruction arising from a charge-density wave. These results will be relevant to understand systems like cuprate and iron-pnictide superconductors [41, 42].

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The research data supporting this publication can be accessed through the University of Bristol data repository [43].

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- [1] J. A. Wilson, F. Di Salvo, and S. Mahajan, Charge-density waves and superlattices in the metallic layered transition metal dichalcogenides, *Adv. Phys.* **24**, 117 (1975).
- [2] J. A. Wilson and A. Yoffe, The transition metal dichalcogenides discussion and interpretation of the observed optical, electrical and structural properties, *Adv. Phys.* **18**, 193 (1969).
- [3] E. Morosan, H. W. Zandbergen, B. S. Dennis, J. W. G. Bos, Y. Onose, T. Klimczuk, A. P. Ramirez, N. P. Ong, and R. J. Cava, Superconductivity in Cu_xTiSe_2 , *Nat. Phys.* **2**, 544 (2006).
- [4] A. F. Kusmartseva, B. Sipos, H. Berger, L. Forró, and E. Tutiš, Pressure Induced Superconductivity in Pristine 1T-TiSe_2 , *Phys. Rev. Lett.* **103**, 236401 (2009).
- [5] X. Xi, L. Zhao, Z. Wang, H. Berger, L. Forró, J. Shan, and K. F. Mak, Strongly enhanced Charge-density-wave order in monolayer NbSe_2 , *Nat. Nanotechnol.* **10**, 765 (2015).
- [6] X. Xi, Z. Wang, W. Zhao, J.-H. Park, K. T. Law, H. Berger, L. Forró, J. Shan, and K. F. Mak, Ising pairing in superconducting NbSe_2 atomic layers, *Nat. Phys.* **12**, 139 (2015).
- [7] B. Singh, C.-H. Hsu, W.-F. Tsai, V. M. Pereira, and H. Lin, Stable charge density wave phase in a 1T-TiSe_2 monolayer, *Phys. Rev. B* **95**, 245136 (2017).
- [8] F. Di Salvo, D. Moncton, and J. Waszczak, Electronic properties and superlattice formation in the semimetal TiSe_2 , *Phys. Rev. B* **14**, 4321 (1976).
- [9] J. A. Wilson, Modelling the contrasting semimetallic characters of TiS_2 and TiSe_2 , *Phys. Status Solidi* **86**, 11 (1978).
- [10] S. Hellmann, T. Rohwer, M. Kalläne, K. Hanff, C. Sohrt, A. Stange, A. Carr, M. M. Murnane, H. C. Kapteyn, L. Kipp, M. Bauer, and K. Rossnagel, Time-domain classification of charge-density-wave insulators., *Nat. Commun.* **3**, 1069 (2012).
- [11] H. Cercellier, C. Monney, F. Clerc, C. Battaglia, L. Despont, M. G. Garnier, H. Beck, P. Aebi, L. Patthey, H. Berger, and L. Forró, Evidence for an Excitonic Insulator Phase in 1T-TiSe_2 , *Phys. Rev. Lett.* **99**, 146403 (2007).
- [12] A. Kogar, M. S. Rak, S. Vig, A. A. Husain, F. Flicker, Y. I. Joe, L. Venema, G. J. MacDougall, T. C. Chiang, E. Fradkin, J. van Wezel, and P. Abbamonte, Signatures of exciton condensation in a transition metal dichalcogenide, *Science* **358**, 1314 (2017).
- [13] H. Hedayat, C. J. Sayers, D. Bugini, C. Dallera, D. Wolfson, T. Batten, S. Karbassi, S. Friedemann, G. Cerullo, J. van Wezel, S. R. Clark, E. Carpena, and E. Da Como, Excitonic and lattice contributions to the charge density wave in 1T-TiSe_2 revealed by a phonon bottleneck, *Phys. Rev. Res.* **1**, 023029 (2019), <http://arxiv.org/abs/1904.05909v1>.
- [14] M. Porer, U. Leierseder, J.-M. Ménard, H. Dachraoui, L. Mouchliadis, I. E. Perakis, U. Heinzmann, J. Demsar, K. Rossnagel, and R. Huber, Non-thermal separation of electronic and structural orders in a persisting charge density wave., *Nat. Mater.* **13**, 857 (2014).
- [15] J. van Wezel, P. Nahai-Williamson, and S. S. Saxena, Exciton-phonon-driven charge density wave in TiSe_2 , *Phys. Rev. B* **81**, 165109 (2010).
- [16] R. Bianco, M. Calandra, and F. Mauri, Electronic and vibrational properties of TiSe_2 in the charge-density-wave phase from first principles, *Phys. Rev. B* **92**, 094107 (2015).
- [17] J. C. E. Rasch, T. Stemmler, B. Müller, L. Dudy, and R. Manzke, 1T-TiSe_2 : Semimetal or Semiconductor?, *Phys. Rev. Lett.* **101**, 237602 (2008).
- [18] M. D. Watson, O. J. Clark, F. Mazzola, I. Marković, V. Sunko, T. K. Kim, K. Rossnagel, and P. D. C. King, Orbital- and k_z -Selective Hybridization of Se $4p$ and Ti $3d$ States in the Charge Density Wave Phase of TiSe_2 , *Phys. Rev. Lett.* **122**, 076404 (2019).
- [19] T. Pillo, J. Hayoz, H. Berger, F. Lévy, L. Schlapbach, and P. Aebi, Photoemission of bands above the Fermi level: The excitonic insulator phase transition in 1T-TiSe_2 , *Phys. Rev. B* **61**, 16213 (2000).
- [20] We use the high-temperature notation of the Brillouin zone throughout the manuscript. In the low-temperature phase the high-temperature L point folds back onto the high-temperature Γ point.
- [21] M. D. Watson, A. M. Beales, and P. D. C. King, On the origin of the anomalous peak in the resistivity of TiSe_2 , *Phys. Rev. B* **99**, 195142 (2019).
- [22] C. Monney, E. F. Schwier, M. G. Garnier, N. Mariotti, C. Didiot, H. Cercellier, J. Marcus, H. Berger, A. N. Titov, H. Beck, and P. Aebi, Probing the exciton condensate phase in 1T-TiSe_2 with photoemission, *New J. Phys.* **12**, 125019 (2010).
- [23] K. Velebit, P. Popčević, I. Batistić, M. Eichler, H. Berger, L. Forró, M. Dressel, N. Barišić, and E. Tutiš, Scattering-dominated high-temperature phase of 1T-TiSe_2 : An optical conductivity study, *Phys. Rev. B* **94**, 075105 (2016).
- [24] G. Li, W. Hu, D. Qian, D. Hsieh, M. Hasan, E. Morosan, R. Cava, and N. Wang, Semimetal-to-Semimetal Charge Density Wave Transition in 1T-TiSe_2 , *Phys. Rev. Lett.* **99**, 027404 (2007).
- [25] I. Taguchi, M. Asai, Y. Watanabe, and M. Oka, Transport properties of iodine-free TiSe_2 , *Physica B+C* **105**, 146 (1981).
- [26] S. H. Huang, G. J. Shu, W. W. Pai, H. L. Liu, and F. C. Chou, Tunable Se vacancy defects and the unconventional charge density wave in $1\text{T-TiSe}_{2-\delta}$, *Phys. Rev. B* **95**, 045310 (2017).
- [27] J. M. Moya, C.-L. Huang, J. Choe, G. Costin, M. S. Foster, and E. Morosan, Effect of synthesis conditions on the electrical resistivity of TiSe_2 , *PRMATERIALS* **3**, 084005 (2019), <http://arxiv.org/abs/1903.12375v2>.
- [28] B. Hildebrand, C. Didiot, A. M. Novello, G. Monney, A. Scarfato, A. Ubaldini, H. Berger, D. R. Bowler, C. Renner, and P. Aebi, Doping Nature of Native Defects in 1T-TiSe_2 , *Phys. Rev. Lett.* **112**, 197001 (2014).
- [29] D. J. Campbell, C. Eckberg, P. Y. Zavalij, H.-H. Kung, E. Razzoli, M. Michiardi, C. Jozwiak, A. Bostwick, E. Rotenberg, A. Damascelli, and J. Paglione, Intrinsic insulating ground state in transition metal dichalcogenide TiSe_2 , *Phys. Rev. Mater.* **3**, 053402 (2019).
- [30] See Supplemental Material [url to be added by editorial team] for details of the two-band analysis on TiSe_2 , which includes Refs. [44] and for details of the Fermi-surface analysis and comparison to complementary work, which includes Refs. [45].
- [31] M. Holt, P. Zschack, H. Hong, M. Y. Chou, and T.-C. Chiang, X-Ray Studies of Phonon Softening in TiSe_2 , *Phys. Rev. Lett.* **86**, 3799 (2001).
- [32] P. Chen, Y.-H. Chan, X.-Y. Fang, S.-K. Mo, Z. Hussain, A.-V. Fedorov, M. Y. Chou, and T.-C. Chiang, Hidden

- Order and Dimensional Crossover of the Charge Density Waves in TiSe_2 , *Sci. Rep.s* **6**, 37910 (2016).
- [33] M.-L. Mottas, T. Jaouen, B. Hildebrand, M. Rumo, F. Vanini, E. Razzoli, E. Giannini, C. Barreteau, D. R. Bowler, C. Monney, H. Beck, and P. Aebi, Semimetal-to-semiconductor transition and charge-density-wave suppression in $1T - \text{TiSe}_{2-x}\text{S}_x$ single crystals, *Phys. Rev. B* **99**, 155103 (2019).
- [34] C. Monney, E. F. Schwier, M. G. Garnier, N. Mariotti, C. Didiot, H. Beck, P. Aebi, H. Cercellier, J. Marcus, C. Battaglia, H. Berger, and A. N. Titov, Temperature-dependent photoemission on $1T\text{-TiSe}_2$: Interpretation within the exciton condensate phase model, *Phys. Rev. B* **81**, 155104 (2010).
- [35] B. Pippard, *Magnetoresistance in Metals*, edited by A. Goldman, P. McClintock, and M. Springford (Cambridge University Press, 1989).
- [36] Y. Xue, Y. Zhang, H. Wang, S. Lin, Y. Li, J.-Y. Dai, and S. P. Lau, Thickness-dependent magnetotransport properties in $1T\text{-VSe}_2$ single crystals prepared by chemical vapor deposition, *Nanotechnology* **31**, 145712 (2020).
- [37] K. Noto, S. Morohashi, K. Arikawa, and Y. Muto, Temperature and magnetic field dependence of the electrical resistance in pure and Fe-doped $2H\text{-NbSe}_2$, *Physica B+C* **99**, 204 (1980).
- [38] M. K. Chan, M. J. Veit, C. J. Dorow, Y. Ge, Y. Li, W. Tabis, Y. Tang, X. Zhao, N. Barišić, and M. Greven, In-Plane Magnetoresistance Obeys Kohler's Rule in the Pseudogap Phase of Cuprate Superconductors, *Phys. Rev. Lett.* **113**, 177005 (2014).
- [39] K. Rossnagel, O. Seifarth, L. Kipp, M. Skibowski, D. Voß, P. Krüger, A. Mazur, and J. Pollmann, Fermi surface of $2H\text{-NbSe}_2$ and its implications on the charge-density-wave mechanism, *Phys. Rev. B* **64**, 235119 (2001).
- [40] V. N. Strocov, M. Shi, M. Kobayashi, C. Monney, X. Wang, J. Krempasky, T. Schmitt, L. Patthey, H. Berger, and P. Blaha, Three-Dimensional Electron Realm in VSe_2 by Soft-X-Ray Photoelectron Spectroscopy: Origin of Charge-Density Waves, *Phys. Rev. Lett.* **109**, 086401 (2012).
- [41] C. Putzke, J. Ayres, J. Buhot, S. Licciardello, N. E. Hussey, S. Friedemann, and A. Carrington, Charge Order and Superconductivity in Underdoped $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ under Pressure, *Phys. Rev. Lett.* **120**, 117002 (2018).
- [42] M. D. Watson, T. Yamashita, S. Kasahara, W. Knafo, M. Nardone, J. Béard, F. Hardy, A. McCollam, A. Narayanan, S. F. Blake, T. Wolf, A. A. Haghighirad, C. Meingast, A. J. Schofield, H. v. Löhneysen, Y. Matsuda, A. I. Coldea, and T. Shibauchi, Dichotomy between the Hole and Electron Behavior in Multiband Superconductor FeSe Probed by Ultrahigh Magnetic Fields, *Phys. Rev. Lett.* **115**, 027006 (2015).
- [43] S. Friedemann, Data accompanying Publication on TiSe_2 magnetotransport study, <https://doi.org/10.5523/bris.1ga60qdfpvsil2ogxvaq14d6ht> (2020).
- [44] K. K. Huynh, Y. Tanabe, T. Urata, S. Heguri, K. Tanigaki, T. Kida, and M. Hagiwara, Mobility spectrum analytical approach for intrinsic band picture of $\text{Ba}(\text{FeAs})_2$, *New Journal of Physics* **16**, 093062 (2014).
- [45] R. A. Craven, F. J. Di Salvo, and F. S. L. Hsu, Mechanisms for the 200 K transition in TiSe_2 : A measurement of the specific heat, *Solid State Commun.* **25**, 39 (1978).